

## Residually finite subrings of the ring of algebraic integers

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**Abstract** - A commutative unitary ring  $A$ , which is neither finite nor a field, is called **residually finite ring** (RF-ring) if the quotient ring  $A/I$  is finite for every nonzero ideal  $I$  of  $A$ . Let  $\mathbf{A}$  be the ring of all algebraic integers, i.e. the set of complex roots of the monic polynomials from  $\mathbb{Z}[X]$ . If  $K$  is a subfield of  $\mathbb{C}$  such that  $[K : \mathbb{Q}] < \infty$ , then the ring  $A = K \cap \mathbf{A}$  is a RF-ring. In this note all the RF-subrings of  $\mathbf{A}$  are determined.

**Key words and phrases** : rings of algebraic integers, residually finite ring, decomposition number, ramification index, residual degree.

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