

# CONCISE REPRESENTATION OF REGULAR LANGUAGES

DANIEL CLAUDIAN VOINESCU<sup>1</sup>

We shall extend/generalize some classical notions such as: quotient of languages to *quotient of languages over a code*, DFAs to *EDFAs*, isomorphism of DFAs to *isomorphism of EDFAs* with the purpose of establishing a more concise way of representing regular languages. We shall also prove that for any given regular language one can effectively find/compute all the EDFAs over the elementary alphabets of  $L$  that recognize  $L$ . In the end we shall give an example to illustrate the new concepts.

**Key words:** combinatorial dimension, combinatorial alphabet, regular language, extended DFA, minimization.

## 1. Introduction

For all the basic/classical notations, definitions and results used in the paper the reader is referred for example to [YuS], [ChKa] and [HaKa].

To get a flavour of how difficult the problems related to combinatorial dimension are, the reader is referred to [Ne1], [Ne2], [Ne3] and [Ne4].

We shall also use in the present paper the following definitions, notations and results introduced/proved in [Voi] and [Voi2]:

• *A combinatorial alphabet of the language  $L$* , see [Voi], is a subset  $A$  of  $\Sigma^*$  for which  $L \subseteq A^*$  and  $card(A) = d(L)$ . The class of all the combinatorial alphabets of the language  $L$  is denoted by  $CA(L)$ , therefore

$$CA(L) = \{A \mid A \subseteq \Sigma^*, L \subseteq A^*, card(A) = d(L)\}$$

• *An elementary alphabet of the language  $L$* , see [Voi2], is an elementary set  $E$  such that  $L \subseteq E^*$  and  $alph_E(L) = E$ .

*The class of all the elementary alphabets of the language  $L$*  will be denoted by  $EA(L)$ , therefore

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<sup>1</sup> The University of Bucharest, Faculty of Mathematics and Informatics.